

Patterns in tri-block copolymers

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We study the Nakazawa-Ohta ternary inhibitory system, which describes domain morphologies in a triblock copolymer as a nonlocal isoperimetric problem for three interacting phase domains. The free energy consists of two parts : the local interface energy measures the total perimeter of the phase boundaries, while a longer-range Coulomb interaction energy reflects the connectivity of the polymer chains and promotes splitting into micro-domains. We consider global minimizers on the two-dimensional torus, in a limit in which two of the species have vanishingly small mass but the interaction strength is correspondingly large. In this limit there is splitting of the masses, and each vanishing component rescales to a minimizer of an isoperimetric problem for clusters in 2D. Depending on the relative strengths of the coefficients of the interaction terms we may see different structures for the global minimizers, ranging from a lattice of isolated simple droplets of each minority species to double-bubbles or core-shells. This represents joint work with S. Alama, X. Lu, and C. Wang [2],[1].

- [1] S. Alama, L. Bronsard, X. Lu, C. Wang. *Periodic minimizers of a ternary non-local isoperimetric problem*. Indiana Univ. Math. J., **70(6)**, 2557–2601, 2021. doi :10.1512/iumj.2021.70.8720.
- [2] S. Alama, L. Bronsard, X. Lu, C. Wang. *Core shells and double bubbles in a weighted nonlocal isoperimetric problem*, 2022, arXiv 221206381.